

# Analytic And Computations



Theorems

Analytic

Computations

Computations2

Others

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## Theorems for 100.



### State Cauchy Integral Formula Formula

$$\frac{n!}{2\pi i} \int_C \frac{f(z)}{(z - z_0)^{n+1}} dz = f^{(n)}(z_0)$$

$$\frac{2\pi i}{n!} \int_C \frac{f(z)}{(z - z_0)^n} dz = f^{(n)}(z_0)$$

$$\int_C \frac{f(z)}{(z - z_0)^n} dz = \frac{2\pi i}{n!} f^{(n)}(z_0)$$

$$\int_C \frac{f(z)}{(z - z_0)^{n+1}} dz = \frac{n!}{2\pi i} f^{(n)}(z_0)$$

none of them

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## Theorems for 200.



What does **Cauchy-Goursat** say?

$f$  analytic,  $C$  simple, then  $\int_C f(z) dz = 0$

$f$  analytic,  $C$  simple, then  $\int_C f(z) dz > 0$

$f$  analytic,  $C$  closed, then  $\int_C f(z) dz < 0$

$f$  analytic,  $C$  simple and closed, then  $\int_C f(z) dz = 0$

$f$  continuous,  $C$  Jordan, then  $\int_C f(z) dz = 0$

$f$  bounded,  $C$  Jordan, then  $\int_C f(z) dz = 0$

## Theorems for 300.



**Louville's Theorem** states that

Any polynomial has no real roots.

Any polynomial has a real root.

Any polynomial with complex coefficients has a real root.

Any polynomial with complex coefficients has no complex roots.

Any polynomial with complex coefficients has at least a complex root.

Any polynomial with real coefficients has at least one complex root.

none of above

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# Theorems for 400.

**De Moivre formula** The roots of  $z^n = re^{i\theta}$  are  $z_k =$

$$r^{1/k} \left[ \cos \left( \frac{\theta + 2\pi n}{k} \right) + i \sin \left( \frac{\theta + 2\pi k}{n} \right) \right], \quad k = 1, \dots, n$$

$$r^{1/k} \left[ \cos \left( \frac{\theta - 2\pi k}{n} \right) + i \sin \left( \frac{\theta + 2\pi k}{n} \right) \right], \quad k = 1, \dots, n$$

$$r \left[ \cos \left( \frac{\theta + 2\pi n}{k} \right) + i \sin \left( \frac{\theta + 2\pi k}{n} \right) \right], \quad k = 1, \dots, n$$

$$r^{1/k} \left[ \cos \left( \frac{\theta + 2\pi k}{n} \right) + i \sin \left( \frac{\theta + 2\pi k}{n} \right) \right], \quad k = 0, \dots, n - 1$$

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## Analytic for 100.



What are the Cauchy Riemann Equations for  $f = u + iv$ ?

$$v_{\theta} = ru_r, \quad u_{\theta} = -rv_r$$

$$v_x = u_y, \quad v_y = -u_x$$

$$v_y = u_x, \quad u_x = -v_y$$

$$v_x = v_y, \quad u_x = -v_y$$

$$v_x = v_y, \quad u_x = -u_y$$

none of them

## Analytic for 200.



What does **holomorphic** mean?

Analytic

$$u_{xx} + u_{yy} = 0$$

Continuous

Differentiable

$$u_x = v_y$$

There is a harmonic conjugate of  $v$   
none of them

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## Analytic for 300.



What does **harmonic** mean?

Analytic

$$u_x x + u_y y = 0$$

Continuous

Differentiable

$$u_x = v_y$$

There is a harmonic conjugate of  $v$   
none of them

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Analytic for 400.



The circle of radius 5 centered at  $-i$  is

$$|z - i|^2 = 5$$

$$|z - i| = 25$$

$$|z - i|^2 = 25$$

$$(x - i)^2 + (y - i)^2 = 25$$

$$|z + i| = 5$$

$$e^{5i} = \theta$$

none of them

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## Computations for 100.



A parametrization of the circle of radius 5 centered at  $-i$  oriented positively is

$$z = 5e^{i\theta}, \quad \theta \in [0, \pi]$$

$$z = e^{5i\theta}, \quad \theta \in [0, 2\pi]$$

$$z = e^{-5i\theta}, \quad \theta \in [0, \pi]$$

$$z = 5e^{i\theta}, \quad \theta \in [0, \pi]$$

$$z = 5e^{i\theta}, \quad \theta \in [0, \pi]$$

$$z = 5e^{i\theta}, \quad \theta \in [2\pi, 4\pi]$$

none of them

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## Computations for 200.



For  $z = re^{i\Theta}$ ,  $\Theta \in (-\pi, \pi)$  the Log of  $z$  is defined to be

$$\ln r + i\Theta + 2\pi k, \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta - 2\pi k, \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta + \pi k, \quad k \in \mathbb{Z}$$

$$\ln r + i(\Theta + \pi k), \quad k \in \mathbb{Z}$$

$$\ln r + 2i(\Theta + \pi k), \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta$$

none of them

## Computations for 300.



For  $z = re^{i\Theta}$ ,  $\Theta \in (-\pi, \pi)$  the  $\log(z)$  is defined to be

$$\ln r + i(\Theta + 2\pi k), \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta - 2\pi k, \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta + \pi k, \quad k \in \mathbb{Z}$$

$$\ln r + i(\Theta + \pi k), \quad k \in \mathbb{Z}$$

$$\ln r + 2i(\Theta + \pi k), \quad k \in \mathbb{Z}$$

$$\ln r + i\Theta$$

none of them

## Computations for 400.



Which number represents  $e^{-3i\pi/2}$ ?

$-i/2$

$2/i$

$i/1$

$-i/1$

$-1/2$

$0/2$

none of them

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Computations2 for 100.



Value of  $e^{i\pi/2}$

i

1

-1

0

-i

none of them

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## Computations2 for 200.



Value of  $i^{2009}$

$i$

$-i$

$-1$

$0$

none of them

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## Computations2 for 300.



Value of principal branch of  $\sqrt{i}$

$$\sqrt{2}/2 - i\sqrt{2}/2$$

$i$

$i^2$

$$\sqrt{2}/2 + i\sqrt{2}/2$$

none of them

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## Computations2 for 400.



In hyperbolic functions?

$$\sinh^2 z + \cosh^2 z = 1$$

$$\sinh^2 z - \cosh^2 z = 1$$

$$\sinh^2 z + \cosh^2 z = 2$$

$$-\sinh^2 z + \cosh^2 z = 1$$

none of them

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Others for 100.



What is a singularity?

A rarity

Something singular

A point where a function is zero

A point for which there is a neighborhood where the function is analytical except at the point

A point where the function vanishes

A point where the function is discontinuous

none of them

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Others for 200.



What is a domain  $D$ ?

Where the function is defined

Where the function is not zero

a set non-empty and connected

They usually tell me

Where I live

none of them

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A function is entire if

it is not broken

it is analytic

it is not rational

it is differentiable everywhere

it is analytic on the complex plane

none of the above

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Others for 400.



What is the Laplace equation?

$$H_{xx}(x, y) + H_{yy}(x, y) = 0$$

$$\int_C f dz = 0$$

$$e^{i\theta} = \cos(\theta) + i \sin(\theta)$$

$$\overline{f(z)} = f(\bar{z})$$

$$e^i + 1 = 0$$

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